PROPOSED TESTS OF CPT SYMMETRY USING D MESONS

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Parameters describing CPT violation are extracted from a variety of rate asymmetries in the neutral-D system. The precision to which these parameters could be measured in present and planned machines is examined.

CPT symmetry is known to be preserved by local, relativistic, point-particle field theories.¹ This symmetry has been experimentally verified to a high degree of accuracy using the neutral-kaon system.² The precision attained in such experiments makes CPT an excellent probe of fundamental particle physics. Additional motivation to search for CPT violation comes from a proposed mechanism through which string theory might lead to violations of CPT at a level comparable to recent experimental bounds.³,4

The interferometric nature of the K system that makes sensitive CPT tests possible is shared by both the D and B systems.^{4–6} In this talk, some prospects for using the D system for CPT tests are briefly described. Further details and our notational conventions can be found in ref. 6.

The D system might naively be viewed as less useful for CPT studies due to the small expected size of the mixing parameter x characterizing the decay time relative to the mixing time. However, the suppression by x of the complex parameter δ_D describing indirect D-system violation can be an advantage in isolating other quantities, including parameters for direct D-system CPT violation and the parameter δ_K for indirect K-system CPT violation. The K-system dependence arises when D decays into neutral kaons are studied.

Two types of experiment are considered: one involving decays of uncorrelated D mesons, and the other involving the production of $\psi(3770)$ with subsequent decay into correlated neutral-D pairs. The variables of experimental interest are asymmetries in decay rates, which have been classified.⁶

An example of an asymmetry isolating δ_D can be constructed from the rates of double-semileptonic decays of correlated D mesons to a final state f in one channel and its charge conjugate \overline{f} in the other:

$$A_{f,\overline{f}} \equiv \frac{\Gamma^{+}(f,\overline{f}) - \Gamma^{-}(f,\overline{f})}{\Gamma^{+}(f,\overline{f}) + \Gamma^{-}(f,\overline{f})} \simeq x(\operatorname{Re}\delta_{D} + 2\operatorname{Im}\delta_{D}) \quad . \tag{1}$$

The superscripts + and - on the decay rates Γ indicate that the decay into f occurs, respectively, before and after the decay into \overline{f} . Note the suppression of δ_D by the factor x.

To obtain an example of an asymmetry involving δ_K for kaons, consider the following combination of total decay rates R_S of uncorrelated D^0 mesons into final states containing K_S and \overline{R}_S of $\overline{D^0}$ mesons into the same final states:

$$A_S \equiv \frac{\overline{R}_S - R_S}{\overline{R}_S + R_S} \quad . \tag{2}$$

The difference between this asymmetry and an analogous one involving K_L final states is

$$A_{L} - A_{S} = -4\operatorname{Re} \delta_{K} + 2\operatorname{Re} (\overline{x}_{K} - x_{K}) + 2x\operatorname{Re} (\epsilon_{D} - \epsilon_{K} - y_{K})$$

$$+4x \left[\operatorname{Im} (\epsilon_{K} + \epsilon_{D}) + \frac{\operatorname{Im} F_{K}}{\operatorname{Re} F_{K}} \right]$$

$$+4x^{2}\operatorname{Re} (\delta_{D} + \delta_{K} - \frac{1}{2}(\overline{x}_{K} - x_{K}))$$

$$-2x^{2}\operatorname{Im} (\delta_{D} - \delta_{K} + \frac{1}{2}(\overline{x}_{K} - x_{K})) . \tag{3}$$

The various quantities in this equation parametrize direct and indirect T and CPT violation in the D and K systems. Applying the condition $x \ll 1$ of small D-system mixing suppresses all but the first two terms, thereby specifically isolating CPT-violating parameters in the K system. The first term, $-4\text{Re}\,\delta_K$, parameterizes indirect CPT violation in the K system. The second term, $2\text{Re}\,(\overline{x}_K - x_K)$, is a measure of simultaneous direct CPT breaking and violation of the $\Delta C = \Delta Q$ rule.

Given an expression for an asymmetry depending on some parameter, the number of events needed to measure that parameter to within one standard deviation σ can be estimated directly if experimental acceptances and backgrounds are neglected. Consider first Eq. 1. The number $N_{\psi(3770)}$ of $\psi(3770)$ events required is determined using the inverse branching ratios of the $\psi(3770)$ into the relevant double-semileptonic final states and summing contributions to the asymmetry. This gives

$$N_{\psi(3770)}(\text{Re }\delta_D + 2\text{Im }\delta_D) \simeq \frac{9}{x^2\sigma^2} \simeq \frac{3600}{\sigma^2}$$
 (4)

The numerator 3600 assumes $x \simeq 0.05$, which is close to the experimental limit and illustrates the best possible scenario for bounding δ_D . The value of x may theoretically be this large if long-distance dispersive effects dominate or if certain extensions of the standard model are invoked.

Next, an estimate is made of the accuracy that can be achieved in the measurement of the parameters in Eq. 3. The inverse branching ratio of the D meson into the relevant final state, which is typically of the order of several percent, is needed as input. The number N_D of uncorrelated D mesons required to measure $\text{Re }\delta_K$ to an accuracy of one standard deviation σ is

$$N_D(\operatorname{Re}\delta_K) \simeq \frac{1}{16\sigma^2 \operatorname{BR}(D^0 \to \overline{K^0} + any)}$$
 (5)

For simplicity, any violations of the $\Delta C = \Delta Q$ rule have been assumed to be independent of direct CPT violation.

Prospects for experimentally studying CPT symmetry using the neutral-D system have been presented. For a sample of 10^8 $\psi(3770)$ events, which could be generated by a τ -charm factory, a theoretical bound could be placed on indirect D-system CPT violation at about the 10^{-2} level if x is large enough. Furthermore, the small size of x can be used to advantage in extracting the parameter δ_K for indirect CPT violation in the K system. Its real part could in principle already be bounded to the 10^{-2} level or better using the currently available 10^5 reconstructed neutral-D events and could be significantly improved in the near future. This provides a different method of measuring δ_K . We remark that it is also possible to extract certain parameters for direct CPT violation in the D system using similar methods.

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